



# Tracking & Calibration Case Studies from AR/VR

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## TRACKING

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- Different tracking technologies
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  - AR Marker tracking
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  - HTC Vive Pro Eye
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- Case Studies on comparing tracking technologies
  - Object tracking
  - Head tracking

## CALIBRATION

### Concept

### Examples of Calibration

- LR based calibration for HRI
- NN based calibration for Auto UI
- NN based calibration for HMDS

# Tracking

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# Concept

## Tracking Technology

### Measurement Principle

- Signal Strength
- Signal Direction
- Time of Flight

### Geometric Property

- Trilateration
- Triangulation

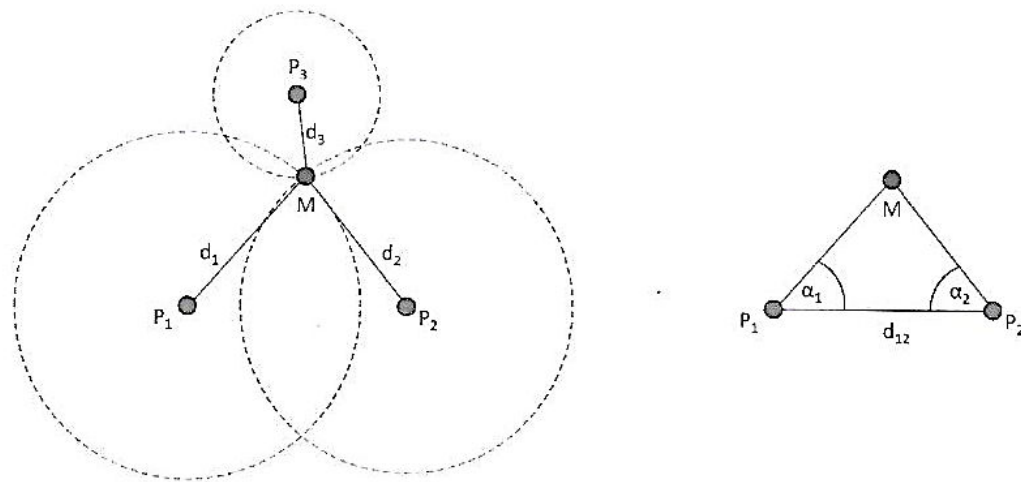
## Sensor Synchronization

### Signal sources

- Active (transmitter / reflector)
- Passive

### DoF

- 3 for position
- 3 for orientation



**Figure 3.4** (left) Trilateration computes the position of a point  $M$  from the known distances  $d_1$ ,  $d_2$ ,  $d_3$  to the points  $P_1$ ,  $P_2$ ,  $P_3$  by intersection of three spheres. (right) Triangulation determines the position of a point  $M$  from two angles  $\alpha_1$  at  $P_1$  and  $\alpha_2$  at  $P_2$  and one known distance  $d_{12}$  between  $P_1$  and  $P_2$ .



# Different Tracking Technologies

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## Imaging Based

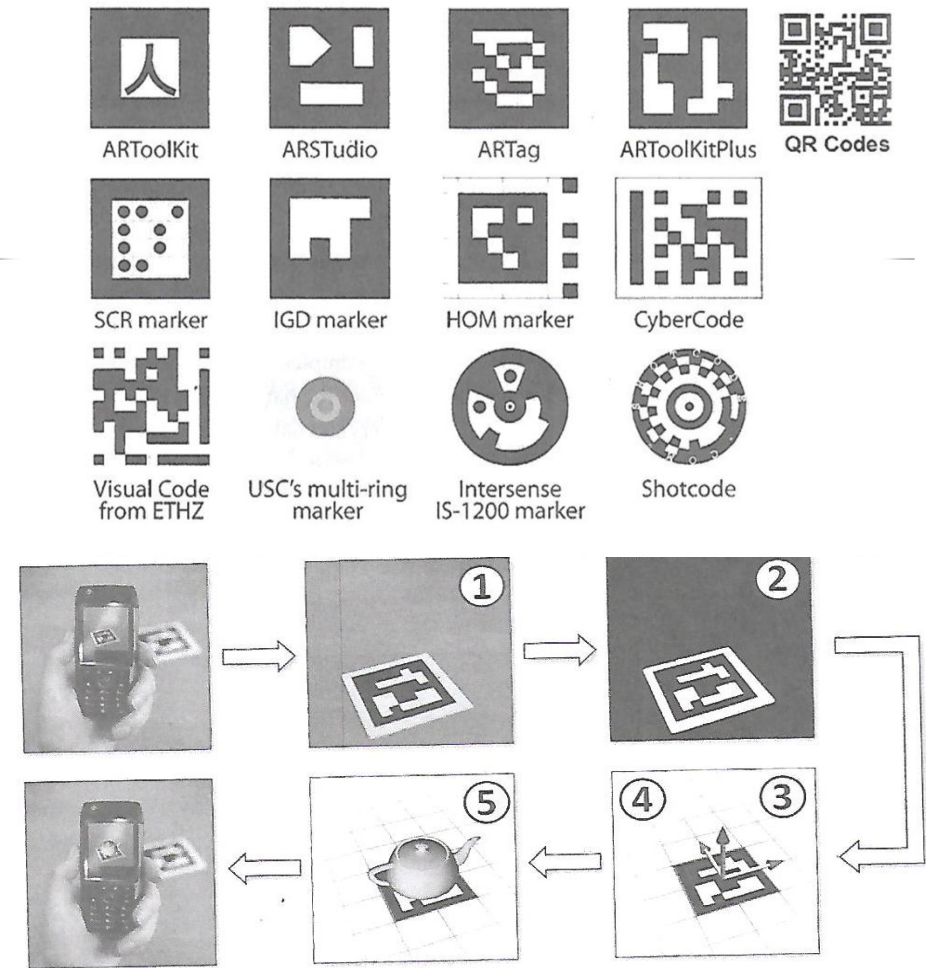
- Frequency of light
- Presence of markers

## Inertial Measurement Units

## Ultrasound

# AR marker tracking

- Circle and Square shapes are easier to detect
- Circle maps to one point, so needs to be grouped
- All corners of square shapes need to be detected
- Patterns inside fiducial markers give orientation and scaling information
- AR renders virtual object after pose estimation of marker



**Figure 4.1** The tracking pipeline for square fiducial markers begins with thresholding the image, followed by quadrilateral fitting and pose estimation. With the recovered pose, AR rendering can be performed. Courtesy of Daniel Wagner.

# OptiTrack – Motion Capture System

IR Camera (850 nm, 120 FPS) – Emits and captures reflections

3M 7610 Retroreflective IR Marker – For effective IR reflection

Precise positioning of markers - On the object to track

Multiple Cameras (8/12/16) can be used to cover the tracking volume

Unreflective / Black background – Desirable

Size of marker – Resolution of camera – Tracking Volume – are important



Markers



# OptiTrack Motion Capture Systems

Calibration - Tracking volume

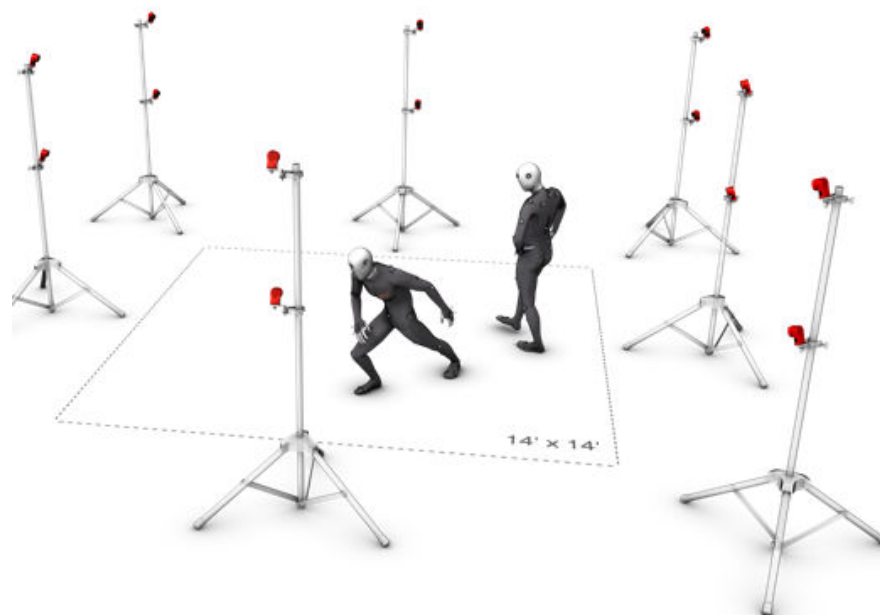
Advanced Image processing algorithms on IR images – 3D localization of markers

Position & Orientation of Rigid Bodies in 3D space & Joint angles and positions in a skeleton

Control and accessing motion capture data – Motive Software/Camera SDK

High accuracy and precision can be obtained subjected to calibration results

Application areas – Movement Sciences, Virtual Reality, Robotics, Drone Tracking, Animation (Film Making), Ergonomic Studies





# IMU based Motion Tracking

Inertial Measurement Units (IMU) are based on inertia.

Ranges from a few square mm (Micro Electro-Mechanical Systems – MEMS) to 50-70 cm diameter (Ring laser gyroscopes)

Unlike Vision based OptiTrack, IMUs are self contained systems

- No reference position in space

Measures linear and angular motion using

- Accelerometers – Measures acceleration in x, y, z axes – Uses seismic mass and Cantilever Beam
- Gyroscopes – Angular velocity around x, y, z axes – Uses vibrating element and Foucault Pendulum

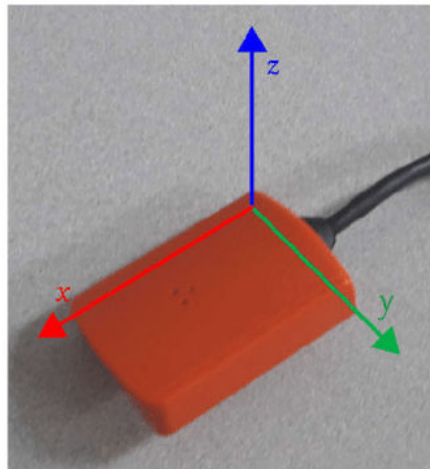
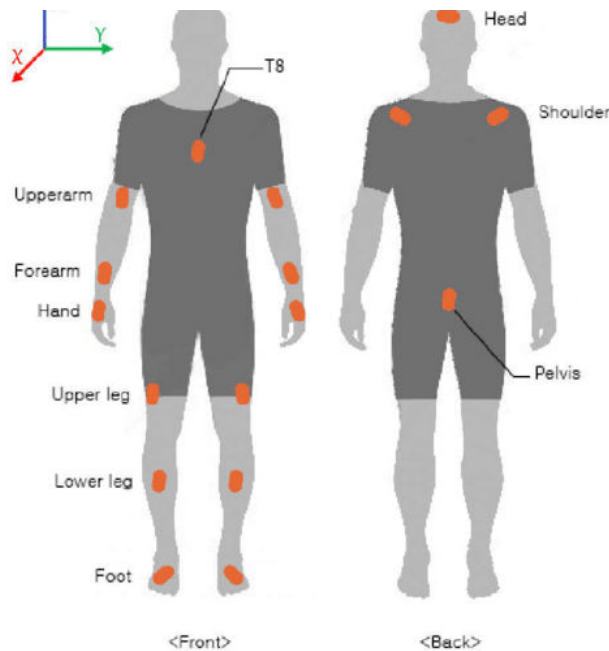
MEMS IMU - Accurate measurements are challenging

- Double integration of accelerometer data – Position
- Integration of gyroscope data – Orientation
- Both are erroneous due to integration constants (Static and Dynamic Errors)
- Hence, we rely on *Magnetometer* – measures magnetic field in x, y, z axes

Factors to obtain high fidelity data

- High sampling rate, Precise sensors
- Calibration of device
- Signal Processing pipeline with Sensor fusion (Kalman Filtering etc.,)

# IMU based Motion Tracking



## Common problems in IMU

- Absolute spatial position cannot be obtained
- Drift in position and orientation data

Recent approaches relies on an array of IMUs to overcome this problems

Xsens Motion Tracking relies on placing 17 IMUs on human to perform accurate motion tracking of various joints

Unlimited tracking range – unlike Optitrack

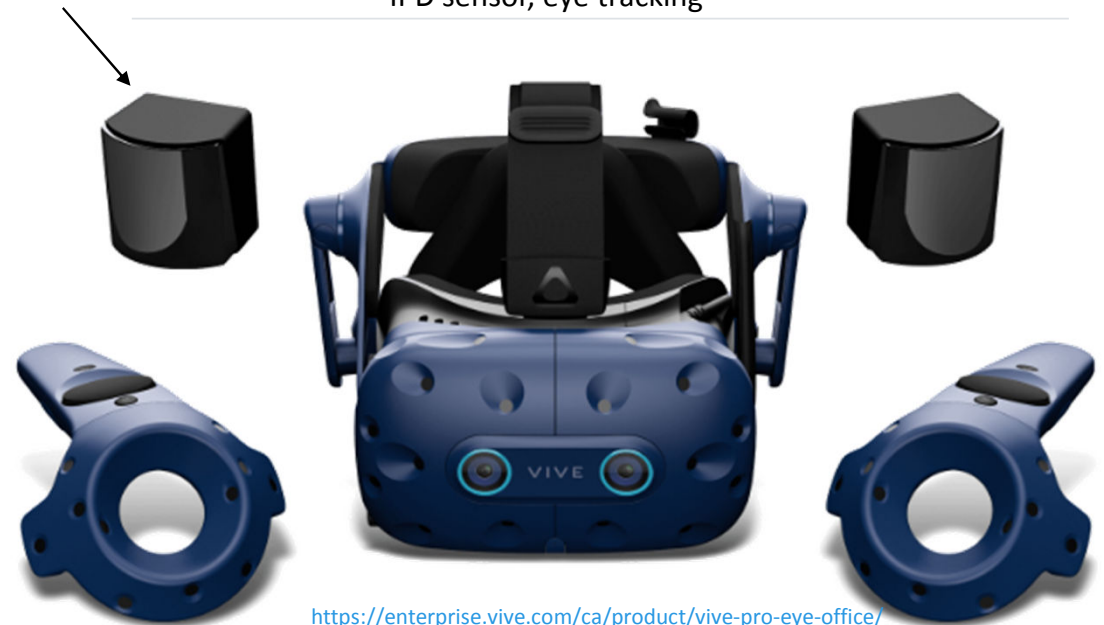
# HTC Vive Pro Eye

- Positional Tracking (6 DoF) – SteamVR ‘Lighthouse’**

*Base stations* emit synced InfraRed(IR) pulses and laser lines that are then picked up by the headset and controllers.

*Headset* contains an array of IR photodiodes connected to a chip. This chip measures the time between the IR flash pulse and being hit by the laser sweep for each axis. Thus, position of tracked device is determined.

Base Station



## Specifications

Screen: Dual OLED 3.5" diagonal

Resolution: 1440 x 1600 pixels per eye (2880 x 1600 pixels combined)

Refresh rate: 90 Hz

Field of view: 110 degrees

Sensors: SteamVR Tracking, G-sensor, gyroscope, proximity, IPD sensor, eye tracking

<https://enterprise.vive.com/ca/product/vive-pro-eye-office/>

# HTC Vive Pro Eye

- Eye Tracking – Tobii Eye Tracking**

Inside of the Head Mounted Display, the eye gaze tracker has illuminator and eye tracking cameras.

The illuminators create a pattern of near infrared light on the eyes. The camera captures high resolution images of the user's eyes. The tracker uses dark pupil tracking with Pupil Center and *Corneal Reflection eye tracking*.

- Foveated Rendering (NVIDIA Turing based GPUs)**

It is a rendering technique which uses eye-gaze of user to render an area inside VR in higher resolution. This also reduces load on Graphics Processor Unit (GPU) significantly.

## Specifications

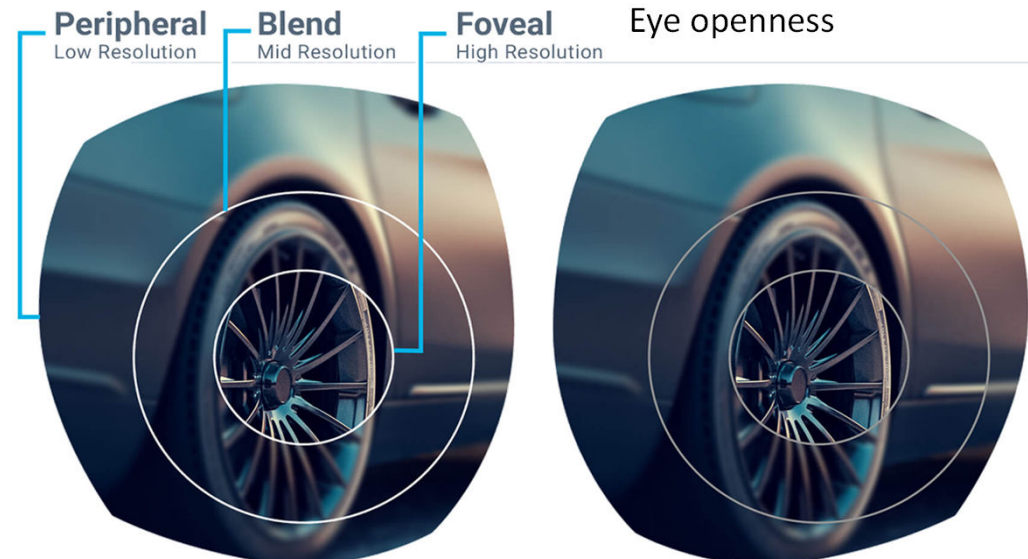
Gaze data output frequency 120Hz  
(binocular):

Accuracy\*: 0.5°–1.1°

Calibration: 5-point

Trackable field of view\*\*: 110°

Data output (eye information): Gaze origin  
Gaze direction  
Pupil position  
Pupil size  
Eye openness



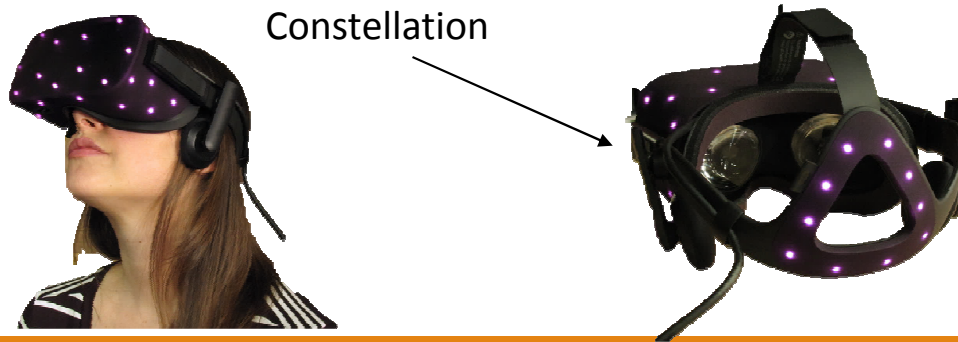
<https://enterprise.vive.com/ca/product/vive-pro-eye-office/>

# Oculus Rift

## Positional Tracking (6 DoF) – ‘Constellation’

Headset and Controllers(Oculus Touch) have a pre-defined pattern(constellation) of infrared LEDs.

*Base Stations*, which are cameras with filters to see only IR light, send images to Computer. Each frame is processed by the computer to identify the position of each IR LED, and thus the relative position of each object.



## Specifications

Screen:	Dual OLED
Resolution:	1080x1200 per eye
Refresh rate:	90 Hz
Field of view:	110 degrees
Sensors:	Accelerometer, Gyroscope, Magnetometer, 360-degree positional tracking



<https://assets.fatllama.com/images/medium/oculus-rift-touch-bundle-51613181.jpg>

# Other Tracking Technologies

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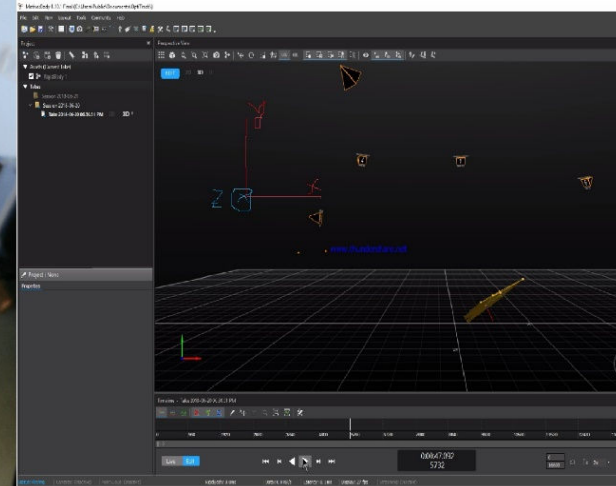
- OpenFace Facial Feature Point Tracking (refer lecture on Alternative Input Modalities)
- Microsoft Kinect (refer lecture on Alternative Input Modalities)
- LeapMotion (refer lecture on Alternative Input Modalities)
- Object tracking through CNN (refer lecture on CNN)
- UltraLeap - Ultrasound based tracking (refer lecture on Haptics)

# Comparison among different tracking technologies

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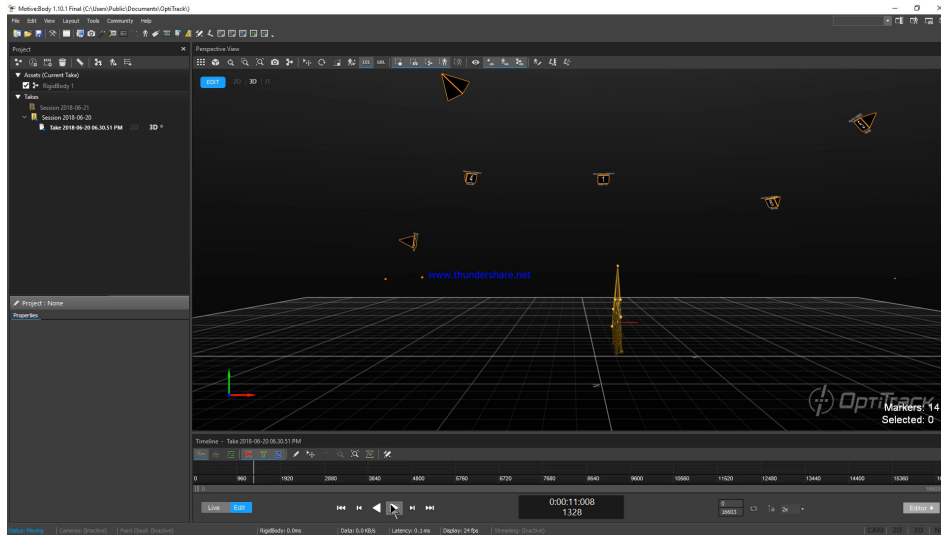


# Object Movement

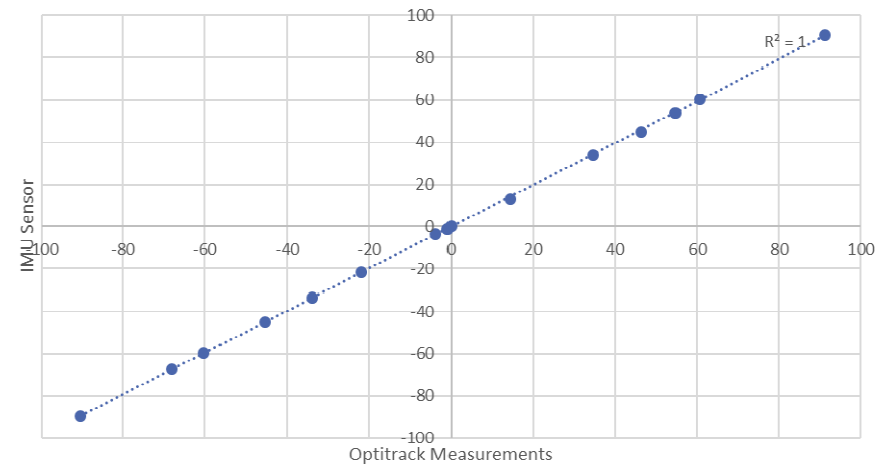




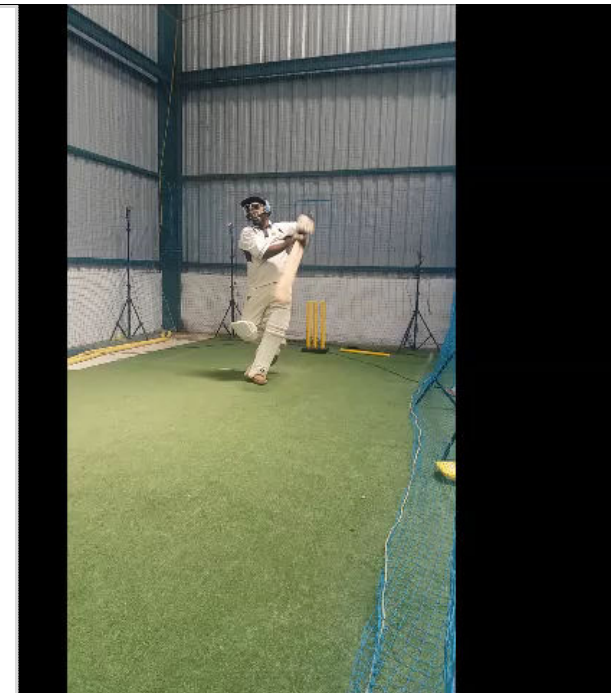
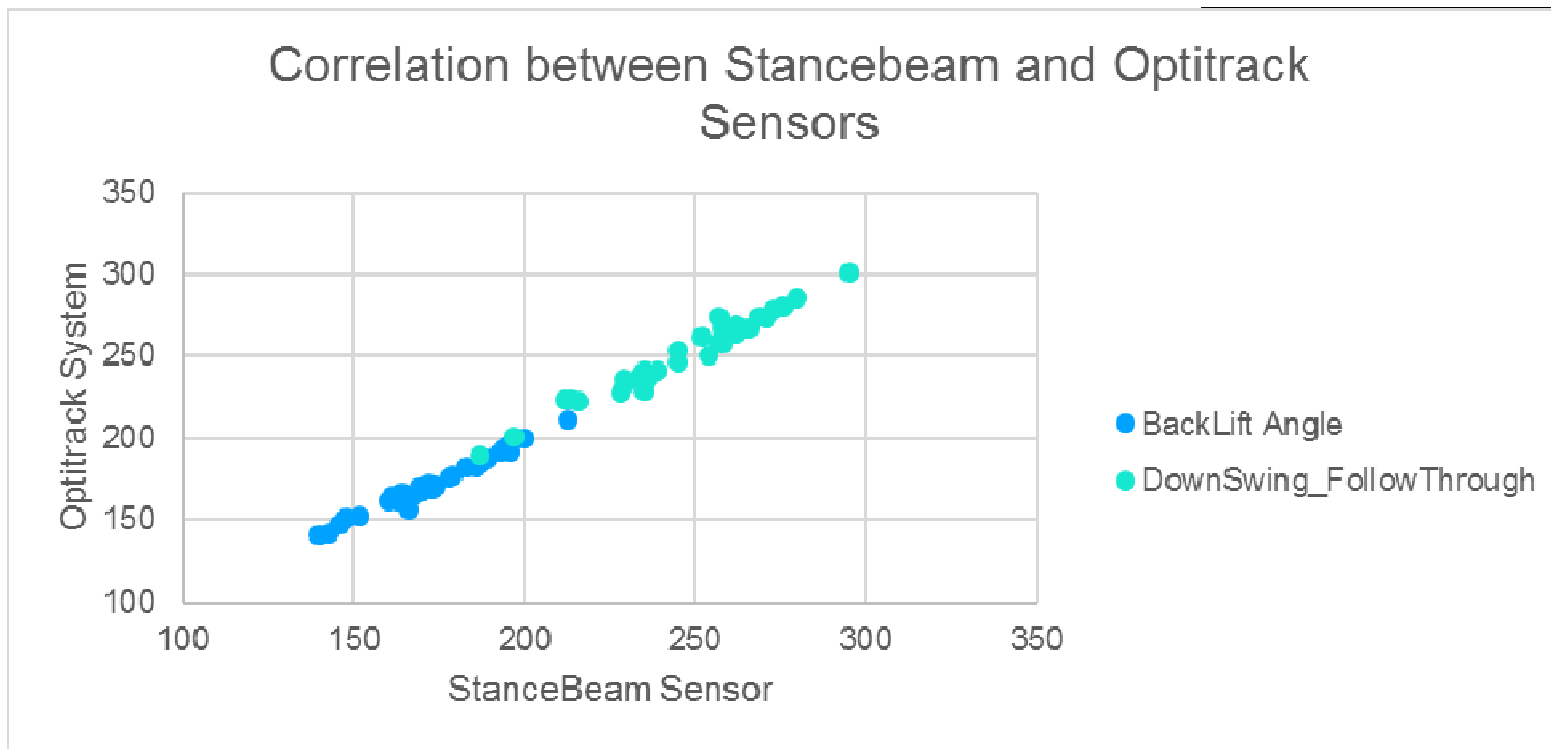
# Static Angle Measurement



Comparing Angles Measured by OptiTrack and IMU Sensor



# Correlation Measurement



# Head Movement

Since the sampling rate of IMU and OptiTrack is different, we performed time sampling and computed the average value for 1 second interval.

We computed correlation value between IMU and OptiTrack using these time average values.

High correlation between IMU and OptiTrack for both yaw (0.85) and pitch (0.77) measurements

Positive, but low correlation (0.4472) for roll measurements



# Calibration

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# Concept

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Camera, Screen and other sensors have different coordinate spaces

Virtual object has to be matched with user input and real object

Mapping between coordinate spaces

Similar to Model or View Transformation used in Computer Vision

Different than camera, sensor or display calibration

# Calibration AR Robotics

Measured coordinates of 9 points in the coordinate space of Robot and screen

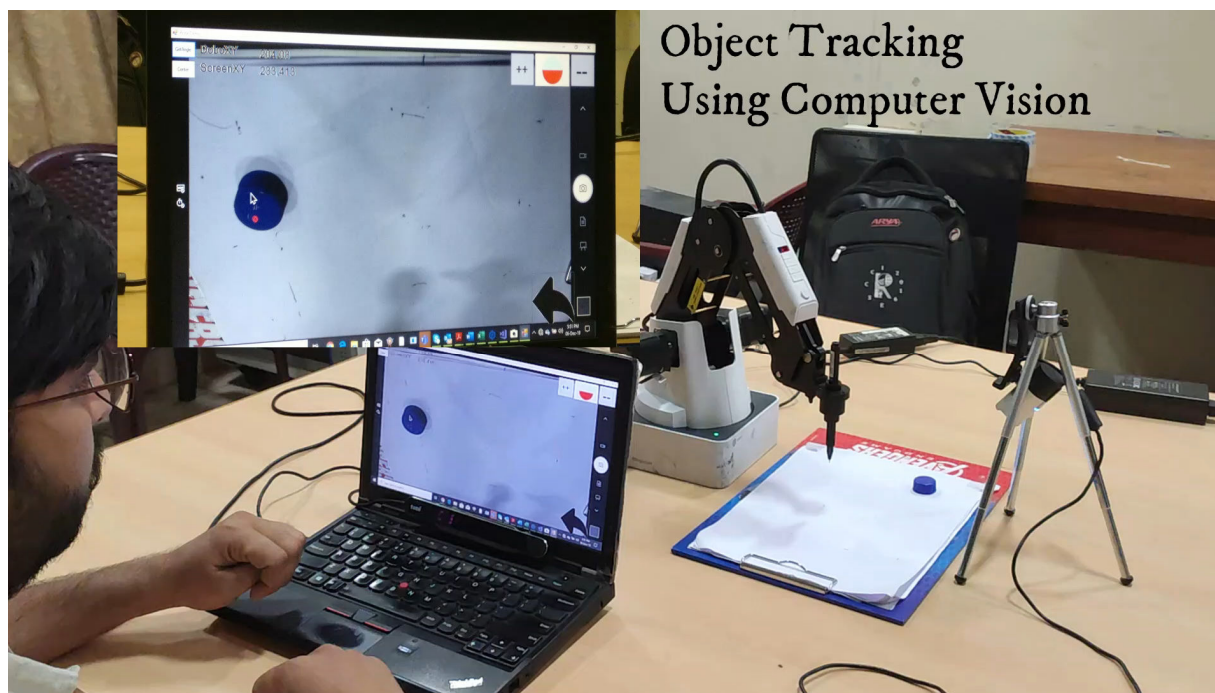
The nine points were distributed throughout the working area of the robot

Used Linear Regression to map screen coordinates to robot coordinates

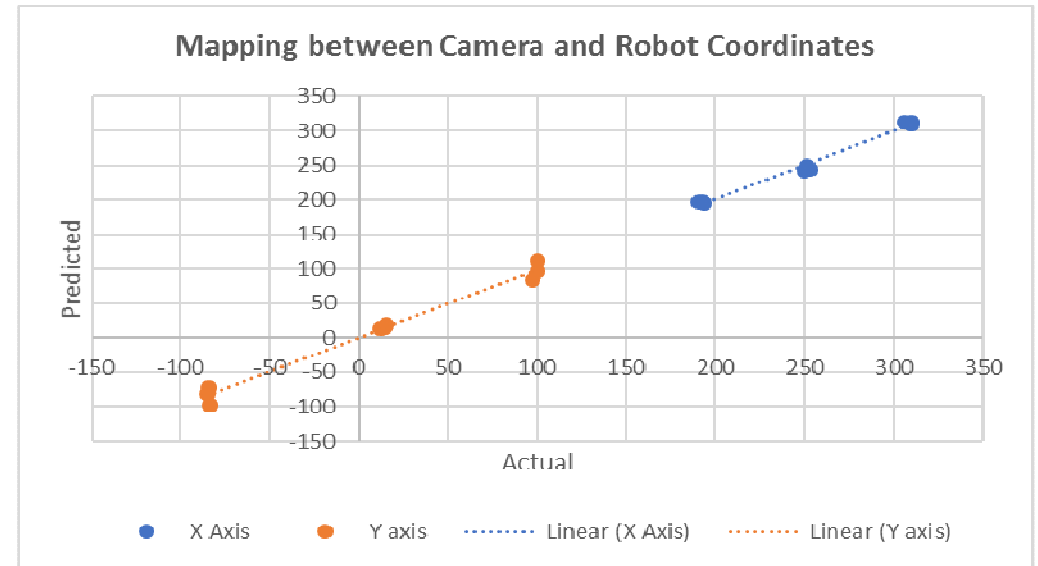
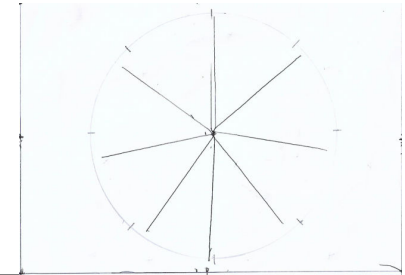
Used correlation and RMS error criteria as goodness of fit

Did not map z-axis

Software takes screen coordinates from user input, converts them to robot coordinate and instruct robot to reach at designated point



# Calibration AR Robotics





# Calibration AutoUI

Existing eye trackers are developed for desktop computing environment where

- Tracker is attached below display
- Display is a flat screen

We used eye tracker to track eyes on windshield

Display was away from eye tracker

Display surface was not flat like a computer screen





# Calibration - AutoUI

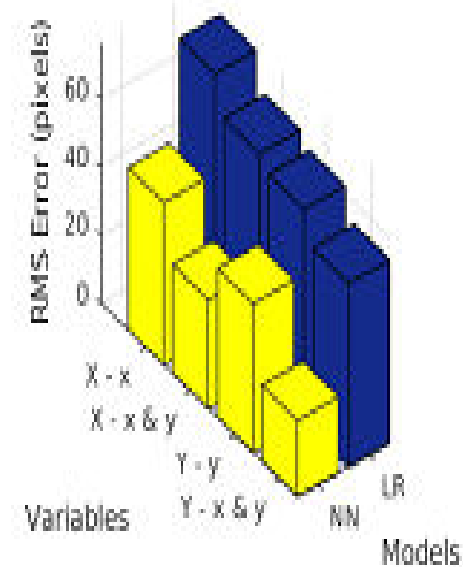
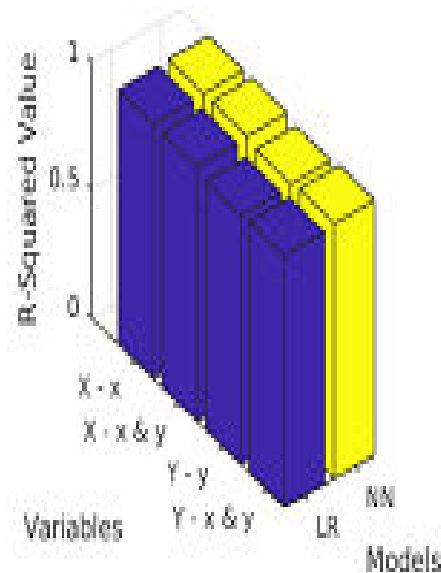
Compared ML systems to convert eye gaze coordinates to screen coordinates on windshield

Set up Linear Regression and Backpropagation Neural Network Models for

- Predicting x-coordinate in screen from x coordinate recorded by gaze tracker
- Predicting x-coordinate in screen from x and y coordinates recorded by gaze tracker
- Predicting y-coordinate in screen from y coordinate recorded by gaze tracker
- Predicting y-coordinate in screen from x and y coordinates recorded by gaze tracker

Compared  $R^2$  and RMS error

Neural Network model worked better than Linear Regression



$R^2$  and RMS error for screen mounted tracker

# Combining Head and Eye Gaze Movements

$$T_z(\alpha) = \begin{pmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$T_y(\beta) = \begin{pmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{pmatrix}$$

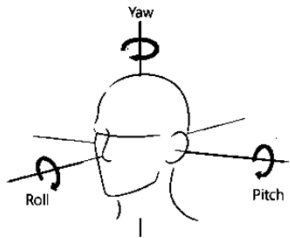
$$T_x(\gamma) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \gamma & -\sin \gamma \\ 0 & \sin \gamma & \cos \gamma \end{pmatrix}$$

$$T = T_z(\alpha)T_y(\beta)T_x(\gamma)$$

$$eyeL_{hc} = TeyeL$$

$$eyeR_{hc} = TeyeR$$

$$eye_{hc} = (eyeL_{hc} \ eyeR_{hc})^T$$



Gaze direction vectors from both eyes (*eyeL* & *eyeR*), with their origins at their respective pupil centers are obtained from eye gaze tracker

9-axis IMU to measure yaw ( $\alpha$ ), pitch ( $\beta$ ) and roll ( $\gamma$ ) of the user's head

Initial head position is the reference co-ordinate axes and measured head orientation accordingly

We performed intrinsic 3D transformation [2] for gaze direction vectors to obtain head compensated gaze vectors (*eyeL<sub>hc</sub>* & *eyeR<sub>hc</sub>*)

# Calibration HMDS

9- Squares appear at designed positions on screen

*Attentive Calibration:* User is asked to focus on each square ; The size of the square reduces in response to user's focus



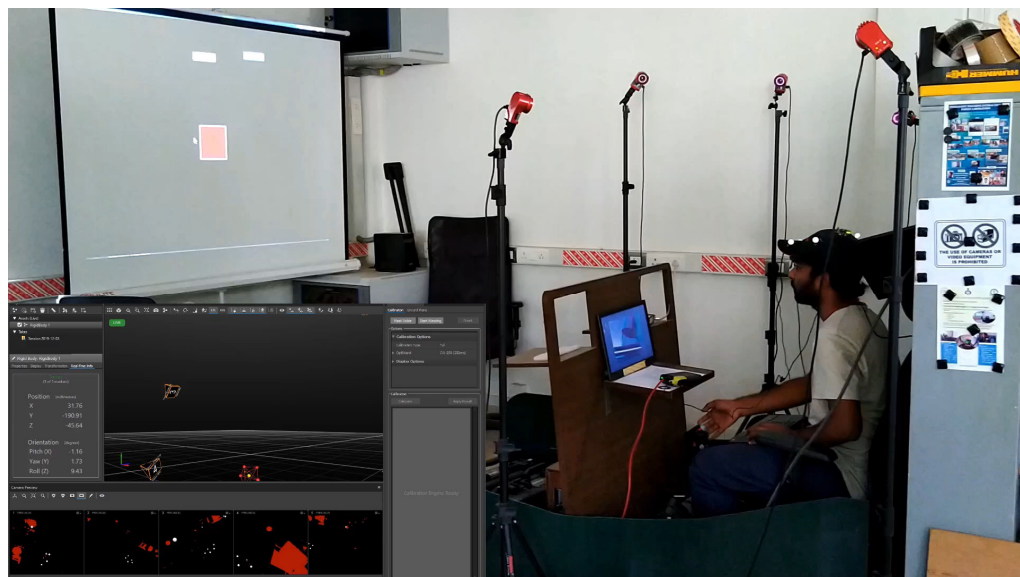
User can use either head or/and gaze to focus on squares; Hence a single calibration routine is enough to obtain head and gaze movements

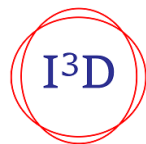
$eye_{hc}$  vectors are collected for each square position at it's minimum size

The mapping function with  $eye_{hc}$  as input and corresponding screen co-ordinates as the output is learnt by training a 2 hidden layer neural network

Loss function: *Mean Squared Error*; Optimizer: *Adam*; Libraries: Tensorflow.NET and Keras.NET

# Demonstration





# We did not cover

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Computer Vision algorithms for tracking

- Needs basic knowledge of Computer Graphics, 3D geometry and computer vision
- Can be described in a separate lecture

AI / ML based tracking algorithms

- Particle filter
- SLAM
- Covered in separate courses

Mobile tracking like GPS

Tracking not commonly used for AR/VR applications like RFID tracking



# Take Away Points

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- Introducing different tracking technologies
- Case studies on commercial AR/VR tracking systems
- Case studies on comparing tracking accuracy
- Mapping virtual and physical coordinates
- Case studies from Robotics, HUD and HMDS